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TITLE OF THE INVENTION

Integrated, Self-Optimizing, Multi-Parameter/Multi-Variable Point-to-Multipoint Communication System [II]

Cross Reference to Related Applications

This application is a continuation-in-part of the following co-pending application:

- Application Serial No.09/475,716, entitled "Integrated Self-Optimizing Multi-Parameter and Multi-Variable Point-to-Multipoint Communication", Express Mail

1 Mailing number EL 524 780 021 US, filed December 30, 1999, Attorney docket num-
2 ber 164.1003.01.

4 BACKGROUND OF THE INVENTION

6 1. *Field of the Invention*

8 This invention relates to wireless communication systems, such as those
9 including adaptive point to multipoint wireless communication.

12 2. *Related Art*

13 Wireless communication between a sender and a receiver includes sending
14 information using a wireless communication link, in which the sender modulates infor-
15 mation onto a wireless communication channel (such as a frequency band reserved for
16 wireless communication between the sender and the receiver), and the receiver demodu-
17 lates that information from the wireless communication channel, so as to recover the
18 original information. The wireless communication link includes multiple physical char-
19 acteristics, including characteristics of the sender's equipment and the receiver's equip-
20 ment, characteristics of objects on or near communication pathways between the sender
21 and the receiver, and characteristics of other communications overlapping communica-
22 tion between the sender and the receiver.

1
2 One problem with known systems is that multiple physical characteristics
3 of the communication link between the sender and receiver can change substantially over
4 relatively short time durations (for example, the distance between the sender and receiver
5 or the equipment used by the sender or receiver). This is particularly so for characteris-
6 tics related to interference, such as co-channel interference (CCI), and for multipath and
7 multipoint effects, such as refraction or reflection resulting in intrasymbol interference
8 and intersymbol interference. Moreover, these multiple physical characteristics can
9 change independently of one another, and can have substantial and relatively unpredict-
10 able effects on one another. Selection of a set of parameters with which to optimize the
11 communication link for one such physical characteristic can therefore be rendered less
12 than optimal by changes in other such physical characteristics. As a result, selection of a
13 single set of such physical characteristics can result in relatively ineffective or inefficient
14 communication between the sender and the receiver.
15

16 Accordingly, it would be advantageous to provide a technique for adaptive
17 point to multipoint wireless communication, in which characteristics of the communica-
18 tion techniques between sender and receiver can be changed adaptively in response to
19 changes in the characteristics of the physical communication media, that is not subject to
20 drawbacks of the known art.
21

SUMMARY OF THE INVENTION

The invention provides a method and system for adaptive point to multi-point wireless communication. The method and system integrate adaptive and dynamic responsiveness for communication parameters related to multiple characteristics of wireless communication links, both for a single sender and a single receiver, and for sets of multiple senders and multiple receivers. Moreover, the method and system are self-optimizing in the sense that they are adaptively and dynamically responsive to results of attempts to optimize parameters related to multiple characteristics of wireless communication links. In a preferred embodiment, multiple characteristics of wireless communication links are optimized simultaneously, in that the optimal set of values for a plurality of N characteristics, rather than N individual optimal values for each characteristic, is adaptively and dynamically selected.

In a first aspect of the invention, a wireless physical (PHY) layer and a wireless media-access-control (MAC) layer collectively include a set of communication parameters, each of which is adaptively modified by a base station controller (BSC) for communication with a plurality of customer premises equipment (CPE). The BSC adjusts communication with each CPE individually and adaptively in response to changes in communication characteristics, including both changes in communication characteristics between the BSC and each selected CPE, and changes in communication characteristics induced by concurrent communication between the BSC and multiple CPE. Particular

1 communication characteristics adapted for can include physical characteristics (such as
2 bit error rate), transport characteristics (such as amount of communication traffic), and
3 application characteristics (such as the nature of an application for the communication
4 traffic).

5
6 In a second aspect of the invention, a wireless transport layer includes
7 adaptive and dynamic characteristics responsive to communication characteristics be-
8 tween the BSC and each selected CPE, and between the BSC and multiple CPE. In a pre-
9 ferred embodiment, these communication characteristics are responsive to each individ-
10 ual communication link so as to optimize communication bandwidth between the BSC
11 and each selected CPE. These include (a) BSC control of a time division multiple access
12 (TDMA) protocol, preferably time division duplex (TDD); (b) BSC control of frequency
13 reuse for CPE, and (c) BSC control of spatial separation of line of sight (LOS), ob-
14 structed line of sight (OLOS), or non-line of sight (NLOS) communication paths with
15 CPE; each responsive to measured bit error rate (BER) and requested communication
16 bandwidth demand. The BSC provides point-to-point and point-to-multipoint wireless
17 communication services using parameters continuously adaptive to current conditions,
18 each individualized to one or more selected CPE.

19
20 The TDD aspect of the wireless transport layer includes burst mode mes-
21 sages from the BSC downstream to individual CPE, and similarly includes burst mode
22 messages from individual CPE upstream to the BSC. This allows the BSC and each indi-

vidual CPE to communicate so as to optimize throughput in a communication direction (downstream or upstream) for each communication link between the BSC and an individual CPE.

The invention provides an enabling technology for a wide variety of applications for communication, so as to obtain substantial advantages and capabilities that are novel and non-obvious in view of the known art. Examples described below primarily relate to a wireless communication system, but the invention is broadly applicable to many different types of communication in which characteristics of the communication link are subject to change.

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 shows a block diagram of a portion of a system using adaptive point to multipoint wireless communication.

Figure 2 shows an example of adaptive frequency reuse provided by the BSC in response to robust modulation at the boundary of a cell or a sector.

Figure 3 shows a chart of reduced bit error rate (BER) and signal to noise (STN) ratio provided by the BSC using antenna selection, antenna polarization selection, and antenna diversity selection.

Figure 4 shows a chart of reduced bit error rate (BER) and signal to interference (STI) ratio provided by the BSC using antenna selection, antenna polarization selection, and antenna diversity selection.

Figure 5 shows a chart of reduced signal to interference (STI) ratio provided by the BSC using power level parameter selection.

Figure 6 shows a chart of reduced bit error rate (BER) ratio provided by the BSC using modulation and symbol rate selection.

Figure 7 shows a chart of reduced outage probability provided by the BSC 120 using modulation and symbol rate selection.

Figure 8 shows a chart of reduced frame loss ratio provided by the BSC 120 using modulation and error code selection.

Figure 9 shows a chart of increased throughput ("goodput") provided by the BSC 120 using message size selection.

Figure 10 shows a chart of increased throughput provided by the BSC 120 using acknowledgement and retransmission parameter selection.

Figure 11 shows a time division duplex frame used in a system as in figure

1.

Figure 12 shows a process flow diagram of a method for operating a system

as in figure 1.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

In the following description, a preferred embodiment of the invention is described with regard to preferred process steps and data structures. Embodiments of the invention can be implemented using general-purpose processors or special purpose processors operating under program control, or other circuits, adapted to particular process steps and data structures described herein. Implementation of the process steps and data structures described herein would not require undue experimentation or further invention.

Related Applications

Inventions described herein can be used in conjunction with inventions described in the following documents.

- U.S. Patent Application Serial No. 09/475,716, Express Mail Mailing No. _____, filed December 30, 1999 in the name of Reza Majidi-Ahy

and Subir Varma, attorney docket number 164.1003.01, titled "Integrated Self-Optimizing Multi Parameter and Multi Variable Point to Multi Point Communication"

- U.S. Patent Application Serial No.09/475,642, Express Mail Mailing No. EL52478001US, filed December 30, 1999 in the name of Subir Varma, Khuong Ngo, Jean Fuentes, Paul Truong, and Reza Majidi-Ahy, attorney docket number 164.1002.01, titled "Adaptive Link Layer for Point to Multipoint Communication System"
- U.S. Patent Application Serial No. 09/540,674, Express Mail Mailing No. EL524781512US: filed March 31, 2000, in the name of Reza Majidi-Ahy, attorney docket number 164.1001.01, titled "Robust Topology Wireless Communication Using Broadband Access Points"

and

- U.S. Patent Application Serial No. _____, Express Mail Mailing No. EL524781225US, filed June 26, 2000, in the name of Reza Majidi-Ahy, attorney docket number 164.1010.01, titled "High-Capacity Scalable Integrated Wireless Backhaul for Broadband Access Networks."

Each of these documents is hereby incorporated by reference as if fully set forth herein. These documents are collectively referred to as the "Incorporated Disclosures."

Lexicography

The following terms refer or relate to aspects of the invention as described below. The descriptions of general meanings of these terms are not intended to be limiting, only illustrative.

- **base station controller (BSC)** — in general, a device for performing coordination and control for a wireless communication cell. There is no particular requirement that the base station controller must be a single device; in alternative embodiments, the base station controller can include a portion of a single device, a combination of multiple devices, or some hybrid thereof.
- **communication link** — in general, an element for sending information from a sender to a recipient. Although in a preferred embodiment the communication links referred to are generally wireless line of sight point to point communication links, there is no particular requirement that they are so restricted.

- 1 • **customer premises equipment (CPE)** — in general, a device for performing
2 communication processes and tasks at a customer location, and operating in con-
3 junction with the base station controller within a wireless communication cell.
4 There is no particular requirement that the customer premises equipment must be a
5 single device; in alternative embodiments, the customer premises equipment can
6 include a portion of a single device, a combination of multiple devices, or some
7 hybrid thereof.
8
- 9 • **IP parameters** — in general, a set of characteristics or parameters relating to an
10 IP layer for a communication link.
- 11 • **media-access-control (MAC) parameters** — in general, with reference to a
12 wireless communication link, a set of characteristics or parameters relating to me-
13 dia access control of a communication link. For example, MAC parameters can
14 include (a) a number of payload data bytes assigned per message, (b) a frequency
15 of acknowledgement messages and a number of message retransmission attempts,
16 (c) a fraction of the communication link allocated to downstream versus upstream
17 communication, and the like.
18
- 19 • **physical (PHY) parameters** — in general, with reference to a wireless communi-
20 cation link, a set of characteristics or parameters relating to physical transmission
21 of information on a communication link. For example, physical characteristics
22

1 can include (a) a symbol transmission rate, (b) a number of payload data bits as-
2 signed per symbol, (c) a number of error detection or correction bits assigned per
3 symbol, and the like.

- 4
- 5 • **QoS parameters** — in general, a set of characteristics or parameters relating to
6 QoS (quality of service) for a communication link.
 - 7
 - 8 • **wireless communication system** — in general, a communication system includ-
9 ing at least one communication link that uses wireless communication techniques.
 - 10 • **wireless transport layer** — in general, a set of protocols and protocol parameters
11 for sending and receiving information using wireless transport. In a preferred em-
12 bodiment, the wireless transport layer is part of a multilayer systems architecture,
13 in which the wireless transport layer is built using a physical transport layer, and
14 the wireless transport layer is used by a logical transport layer such as IP.
 - 15

16

17 As noted above, these descriptions of general meanings of these terms are
18 not intended to be limiting, only illustrative. Other and further applications of the inven-
19 tion, including extensions of these terms and concepts, would be clear to those of ordi-
20 nary skill in the art after perusing this application. These other and further applications
21 are part of the scope and spirit of the invention, and would be clear to those of ordinary
22 skill in the art, without further invention or undue experimentation.

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System Context

The context of the invention is similar to that of the Incorporated Disclosures.

A system using adaptive point to multipoint wireless communication in a wireless communication system operates as part of a system in which devices coupled to a network (such as a computer network) send messages, route and switch messages, and receive messages. In a preferred embodiment, devices coupled to (and integrated with) the network send, route, and receive these messages as sequences of packets, each of which has a header including delivery information and a payload including data. In a preferred embodiment, packet format conforms to the OSI model, in which an application protocol (layer 5, such as FTP), uses a transport protocol (layer 4, such as TCP), which uses a network protocol (layer 3, such as IP), which uses a media access control (MAC) protocol (layer 2), which uses a physical transport technique (layer 1).

The system using adaptive point to multipoint wireless communication is described herein with regard to layer 1 and layer 2, particularly as it applies to interactions between layer 1 and layer 2 and between those layers and layer 3. However, concepts and techniques of the invention are also applicable to other layers of the OSI model. The application gives examples of cases where the type of application in the application

1 layer (layer 5) could be incorporated into embodiments of the invention to improve
2 communication. Adapting those concepts and techniques to such other layers would not
3 require undue experimentation or further invention, and is within the scope and spirit of
4 the invention.

5
6 *System Elements*

7
8 Figure 1 shows a block diagram of a portion of a system using adaptive
9 point to multipoint wireless communication.

10
11 A system 100 includes a wireless communication cell 110 (or a portion
12 thereof), a base station controller (BSC) 120, one or more customer premises equipment
13 (CPE) 130, and one or more (possibly partially) interfering or reflecting obstacles 140.
14
15

16 The wireless communication cell 110 (not shown) includes a generally
17 hexagon-shaped region of local surface area, such as might be found in a metropolitan
18 region. Use of generally hexagon-shaped regions is known in the art of wireless commu-
19 nication because they are able to tile a local region with substantially no gaps. However,
20 although in a preferred embodiment the wireless communication cell 110 includes a gen-
21 erally hexagon-shaped region, there is no particular requirement for using that particular
22 shape; in alternative embodiments it may be useful to provide another shape or tiling of
the local surface area.

1
2 In figure 1, a portion of the cell 110, herein called a "sector" 111, includes a
3 generally triangular-shaped region of local surface area, disposed so that a set of six sec-
4 tors 111 are combined to form a single cell 110. Thus, the BSC 120 is disposed at or near
5 one corner of the sector 111, while CPE 130 are disposed within the sector 111. Moreo-
6 ver, obstacles 140 are disposed within the sector 111 or at junctions of multiple sectors
7 111.

8
9 Although the invention is primarily described with regard to a single sector
10 111, there are substantial applications of the invention to interaction between multiple
11 sectors 111 within a cell 110, and to interaction between sectors 111 in multiple cells
12 110. These substantial applications of the invention are described at least in part in this
13 application. Moreover, other and further substantial applications of the invention with
14 regard to multiple sectors 111, both within a single cell 110 and among multiple cells
15 110, would be clear to those skilled in the art of wireless communication after perusal of
16 this application, and would not require undue experimentation or further invention.

17
18 The BSC 120 includes a processor, program and data memory, mass stor-
19 age, and one or more antennas for sending or receiving information using wireless com-
20 munication techniques.

1 Similar to the BSC 120, each CPE 130 includes a processor, program and
2 data memory, mass storage, and one or more antennas for sending or receiving informa-
3 tion using wireless communication techniques.
4

5 Obstacles 140 might include buildings, other construction, electromagneti-
6 cally active elements such as radio transmitters and repeaters, other electromagnetic ele-
7 ments such as power lines or weather effects, and mobile objects such as vehicles.
8

9 Mobile objects can serve as obstacles, due to their electromagnetic charac-
10 teristics, size, or other features. For example, a car or truck can present an obstacle that
11 dampens or prevents transmission of wireless communication. Similarly, an airplanes,
12 dirigibles, or trucks can present surfaces with continual or intermittent reflective features,
13 possibly leading to multipath effects. Moving obstacles 140 can present substantial
14 variation over time in characteristics of communication links between the BSC 120 and
15 selected CPE 130.
16

17 Similarly, non-moving obstacles 140 can also present substantial variation
18 over time in characteristics of communication links between the BSC 120 and selected
19 CPE 130. For example, the electromagnetic reflectivity characteristics of a building
20 might vary with regard to power usage in the building, ambient temperature, and other
21 factors.
22

1 Other and further substantial applications of the invention with regard to
2 both moving and non-moving obstacles 140, both within a single cell 110 and among
3 multiple cells 110, would be clear to those skilled in the art of wireless communication
4 after perusal of this application, and would not require undue experimentation or further
5 invention.

6
7 Communication among devices within the wireless communication cell 110
8 is preferably conducted on a one-to-one basis between each CPE 130 and the BSC 120.
9 Thus, the BSC 120 communicates with each CPE 130, and each CPE 130 communicates
10 with the BSC 120. In a preferred embodiment, CPE 130 do not communicate directly
11 with other CPE 130. However, in alternative embodiments, CPE 130 may communicate
12 directly with other CPE 130, with the characteristics of such communication being con-
13 trolled either by the BSC 120, by one CPE 130 selected by the BSC 120, or by one CPE
14 130 mutually agreed to among the communicating CPE 130.

15
16 Communication between the BSC 120 and each CPE 130 is conducted us-
17 ing a TDD technique, in which time durations are divided into repeated individual
18 frames, each one of which includes a “downstream” portion and an “upstream” portion.
19 Unlike existing protocols in which transmissions are controlled by the transmitting side,
20 the BSC 120 controls transmissions for both upstream and downstream directions, with-
21 out specific requests from CPE 130.

1 During the downstream portion of each frame, the BSC 120 transmits, thus
2 sending information to one or more CPE 130. During the upstream portion of each
3 frame, each CPE 130 is potentially allocated a time slot for transmission, thus for sending
4 information to the BSC 120. TDD techniques are known in the art of wireless communi-
5 cation.

7 *Adaptive Point to Multipoint Communication*

8
9 The BSC 120 maintains a set of physical (PHY) parameters and media-
10 access-control (MAC) parameters for each CPE 130. In a preferred embodiment, control
11 of each parameter by the BSC 120 is independent and individual with regard to each CPE
12 130. Thus for example, the BSC 120 determines power level and modulation type for
13 each CPE 130 without regard to power level and modulation type for any other CPE 130.
14 Similarly, the BSC 120 determines power level for a particular CPE 130 without regard
15 for modulation type for that particular CPE 130.

16
17 However, in alternative embodiments, the BSC 120 may control multiple
18 parameters in groups, or in a correlated manner. Thus, the BSC 120 may alternatively
19 determine power level and modulation type for a particular CPE 130 as a pair of values,
20 where the pair of values is determined so that an optimal pair (rather than optimal indi-
21 vidual values) is selected. For example, the BSC 120 may notice that a particular CPE
22 130 needs substantially less transmission power level when using a more robust modula-

tion type, and thus select the power level and modulation type parameters for that particular CPE 130 jointly so as to be optimal as a pair, rather than as individual values.

In further alternative embodiments, the BSC 120 may control parameters for multiple CPE 130 in groups, or in a correlated manner. Thus, the BSC 120 may alternatively select a group of more than one CPE 130 and control physical parameters and MAC parameters for the group as a whole, where the parameters are determined so as to be optimal for the group, rather than for individual CPE 130. For example, the BSC 120 might notice that two CPE 130 A and B can generate substantial co-channel interference under selected conditions, and therefore set the channel selection parameters for those two CPE 130 A and B to avoid that co-channel interference.

As a further alternative embodiment of controlling parameters for multiple CPE 130 in groups, the BSC 120 may control parameters so that (for a group of N CPE 130), some portion M of those CPE 130 have a first set of parameters, while some other portion (N - M) of those CPE 130 have a second set of parameters, so that communication with the entire group of N CPE 130 is optimal. For example, the BSC 120 may determine, for N = 10 CPE 130, that M = 9 of those CPE 130 communicate with the BSC 120 at 20 megasymbols per second, while the remaining (N - M) = 1 of those CPE 130 communicate with the BSC 120 at 5 megasymbols per second, so that allocated resources are minimized for communication with the entire group of N = 10 CPE 130.

1 In a preferred embodiment, each of the following parameters actually has
2 two values: a first value for transmission by the BSC 120 and a second value for trans-
3 mission by the CPE 130. Thus, the BSC 120 can transmit using a first set of parameters
4 while the CPE 130 is instructed to transmit using a second set of parameters. There is no
5 particular requirement that the first set of parameters and the second set of parameters
6 need be correlated, except for optimizations desirable due to the nature of the communi-
7 cation link between the BSC 120 and the CPE 130.

8
9 In alternative embodiments, the optimizations selected by the BSC 120 may
10 be responsive to optimizations or requirements imposed by higher levels in the OSI
11 model. For example, there are instances noted below in which, if the application level is
12 transmitting voice information or other streaming media, a first set of parameters would
13 be considered optimal; while if the application level is transmitting file data or other rela-
14 tively cohesive information, a second set of parameters would be considered optimal.

15
16 *Preferred Parameters*

17
18 Figure 2 shows an example of adaptive frequency reuse provided by the
19 BSC in response to robust modulation at the boundary of a cell 110 or a sector 111.

20
21 The BSC 120 optimizes its communication link with each selected CPE
22 130 so as to provide (a) robust link performance, (b) avoidance of interference, (c) avoid-

1 ance of multipath effects, (d) amelioration of obstructed or partially obstructed LOS, so
2 as to maximizing bandwidth throughput to each selected CPE 130.

3
4 The BSC 120 notes the effect of frequency separation between pairs of CPE
5 130, so as to optimize frequency division multiple access (FDMA), such as frequency di-
6 vision duplex (FDD) techniques. For example, in a preferred embodiment, the BSC 120
7 provides for spatially closer frequency reuse when relatively lesser frequency separation
8 between pairs of CPE 130 is adequate to provide sufficient communication bandwidth.

9
10 Similarly, the BSC 120 notes the effect of both spatial and frequency sepa-
11 ration between pairs of CPE 130, so as to optimize time division multiple access
12 (TDMA), such as time division duplex (TDD) techniques. For example, in a preferred
13 embodiment, the BSC 120 provides for temporal allocation of each TDD frame when
14 relatively lesser temporal separation between pairs of CPE 130 is adequate to provide
15 sufficient communication bandwidth.

16 In alternative embodiments, the BSC 120 may note the effect of spatial,
17 frequency and time separation between pairs of CPE 130, so as to optimize code division
18 multiple access (CDMA), or other spread spectrum techniques, or other techniques avail-
19 able for sharing communication channels among a plurality of communicating entities.

20
21 In a preferred embodiment, physical parameters and MAC parameters in-
22 clude at least the following physical parameters:

- 1
- 2 • **antenna selection** — The BSC 120 includes more than one antenna, and each
- 3 CPE 130 includes one or more antennas. In a preferred embodiment, the antenna
- 4 selection parameter includes a choice of which one antenna at the BSC 120 and
- 5 which one antenna at the each CPE 130.
- 6

7 The antenna selection parameter allows the BSC 120 to optimize a communication

8 link with a selected CPE 130 in response to both interference effects and multipath

9 effects.

10 In a preferred embodiment, the antenna selection parameter is supplemented using

11 an antenna polarization parameter. The antenna selection parameter allows the

12 BSC 120 to optimize a communication link with a selected CPE 130 in response to

13 both interference effects and multipath effects.

14

15

16 In alternative embodiments, the antenna selection parameter includes the possibil-

17 ity of sending portions of communication signal from each of a plurality of anten-

18 nas (thus, either simultaneously sending from two antennas or sending from one

19 antenna followed by a second antenna) and similarly receiving portions of com-

20 munication signal at each of a plurality of antennas.

21

Figure 3 shows a chart of reduced bit error rate (BER) and signal to noise (STN) ratio provided by the BSC using antenna selection, antenna polarization selection, and antenna diversity selection.

A chart 300 includes an X-axis 310 representing a signal to noise (STN) ratio, a Y-axis 320 representing a bit error rate (BER) value, and a set of plotted curves 330 each representing a function coupling STN on the X-axis 310 with BER on the Y-axis 320 for a selected value of an antenna diversity selection parameter (labeled L = diversity order in figure 3).

In a preferred embodiment, the BSC 120 selects, for each communication link with selected CPE 130, an antenna diversity selection parameter for the communication link. It would be clear to those of ordinary skill in the art, after perusal of this application, that selection of the antenna diversity selection parameter, and other antenna selection parameters, is a tool for the BSC 120 to maximize the value of its communication link with each selected CPE 130.

Figure 4 shows a chart of reduced bit error rate (BER) and signal to interference (STI) ratio provided by the BSC 120 using antenna selection, antenna polarization selection, and antenna diversity selection.

A chart 400 includes an X-axis 410 representing a signal to interference (STI) ratio, a Y-axis 420 representing a bit error rate (BER) value, and a set of plotted

curves 430 each representing a function coupling STI on the X-axis 410 with BER on the Y-axis 420 for a selected value of an antenna diversity selection parameter (labeled L = diversity order in figure 3).

In a preferred embodiment, the BSC 120 selects, for each communication link with selected CPE 130, an antenna diversity selection parameter for the communication link. It would be clear to those of ordinary skill in the art, after perusal of this application, that selection of the antenna diversity selection parameter, and other antenna selection parameters, is a tool for the BSC 120 to maximize the value of its communication link with each selected CPE 130.

- **power level** — The BSC 120 sets the power allocated for transmission.

The power level parameter allows the BSC 120 to optimize a communication link with a selected CPE 130 in response to interference effects.

Figure 5 shows a chart of reduced signal to interference (STI) ratio provided by the BSC 120 using power level parameter selection.

A chart 500 includes an X-axis 510 representing a distance from interference source, a Y-axis 520 representing a signal to interference (STI) ratio, and a set of plotted curves 530 each representing a function coupling distance from interference

1 source on the X-axis 510 with STI on the Y-axis 520 for a selected value of an antenna
2 diversity selection parameter (labeled L = diversity order in figure 3). A first curve 530
3 shows a relationship function without power level selection by the BSC 120; a second
4 curve 530 shows a relationship function with power level selection by the BSC 120 si-
5 multaneously at both the BSC 120 and the selected CPE 130; and a third curve 530 shows
6 a relationship function with power level selection by the BSC 120 independently at each
7 of the BSC 120 and the selected CPE 130.

8
9 In a preferred embodiment, the BSC 120 selects, for each communication
10 link with selected CPE 130, a power level selection parameter for the communication
11 link. It would be clear to those of ordinary skill in the art, after perusal of this applica-
12 tion, that selection of the power level selection parameter, is a tool for the BSC 120 to
13 maximize the value of its communication link with each selected CPE 130.

- 14
15 • **channel selection** — The communication link includes more than one frequency
16 channel on which transmissions are sent and received. In a preferred embodiment,
17 the channel selection parameter includes a choice of which one channel the BSC
18 120 uses to transmit and which one channel the each CPE 130 transmit.

19
20 The channel selection parameter allows the BSC 120 to optimize a communication
21 link with a selected CPE 130 in response to both interference effects and multipath
22 effects.

Similar to antenna selection, in alternative embodiments, the channel selection parameter includes the possibility of sending portions of communication signal from each of a plurality of channels (thus, either simultaneously sending from two channels or sending from one channel followed by a second channel) and similarly receiving portions of communication signal at each of a plurality of channels.

In alternative embodiments, the communication link may include other types of channel other than frequency division (FDMA), such as spread spectrum code division (CDMA), or some combination of transmission separation techniques, such as a combination of CDMA, FDMA, and TDMA techniques. In such alternative embodiments, the channel selection parameter includes the possibility of selecting one or more of such separation techniques either independently or jointly.

- **modulation type** — The BSC 120 and the CPE 130 can exchange information at one of a number of different bit per symbol rates, as determined by the modulation type for transmission of information. In a preferred embodiment, the modulation type parameter selects between QPSK, 16QAM, and 64QAM modulation techniques. When the modulation type is QPSK, two bits are transmitted for each symbol. Similarly, when the modulation type is 16QAM, four bits are transmitted for each symbol, and when the modulation type is 64QAM, six bits are transmitted for each symbol.

1
2 The modulation selection parameter allows the BSC 120 to optimize a communi-
3 cation link with a selected CPE 130 in response to both interference effects and
4 multipath effects.

5
6 In alternative embodiments, the modulation type may include other techniques for
7 modulation, such as QFSK or other frequency modulation techniques, spread
8 spectrum modulation techniques, or some combination thereof.

9
10 Figure 6 shows a chart of reduced bit error rate (BER) ratio provided by the
11 BSC using modulation and symbol rate selection.
12

13 A chart 600 includes an X-axis 610 representing a C/I_C ratio in decibels
14 (db), a Y-axis 620 representing a bit error rate (BER), and a set of plotted curves 630
15 each representing a function coupling C/I_C ratio on the X-axis 610 with BER on the Y-
16 axis 620 for a selected value of a modulation parameter. The modulation parameter can
17 vary among $1/4$ -QPSK, $1/2$ -QPSK, QPSK, 16QAM, and 64QAM.
18

19 In a preferred embodiment, the BSC 120 selects, for each communication
20 link with selected CPE 130, a modulation selection parameter for the communication
21 link. It would be clear to those of ordinary skill in the art, after perusal of this applica-

tion, that selection of the modulation and symbol rate selection parameter, is a tool for the BSC 120 to maximize the value of its communication link with each selected CPE 130.

Figure 7 shows a chart of reduced outage probability provided by the BSC 120 using modulation and symbol rate selection.

A chart 700 includes an X-axis 710 representing a normalized delay spread between symbols, a Y-axis 720 representing a C/I_C ratio in decibels (db), and a set of plotted regions 730 each representing a function coupling normalized delay spread on the X-axis 710 with C/I_C ratio on the Y-axis 720 for a selected value of a modulation and symbol rate parameter. The modulation parameter can vary among $\frac{1}{4}$ -QPSK, $\frac{1}{2}$ -QPSK, QPSK, 16QAM, and 64QAM.

In a preferred embodiment, the BSC 120 selects, for each communication link with selected CPE 130, a modulation and symbol rate selection parameter for the communication link. It would be clear to those of ordinary skill in the art, after perusal of this application, that selection of the modulation and symbol rate selection parameter, is a tool for the BSC 120 to maximize the value of its communication link with each selected CPE 130.

- **symbol rate** — The BSC 120 and the CPE 130 can exchange information at one of a number of different symbol per second rates, as determined by the symbol

1 rate for transmission of information. In a preferred embodiment, the symbol rate
2 parameter selects between transmission rates of five, ten, or twenty megasymbols
3 per second.

4
5 The symbol rate parameter allows the BSC 120 to optimize a communication link
6 with a selected CPE 130 in response to both interference effects and multipath ef-
7 fects.

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- **error code type** — The BSC 120 and the CPE 130 can exchange information using one of a number of different error detection and correction techniques. These error detection and correction techniques can include past error detection and correction and forward error detection and correction. Various codes and techniques for error detection and correction are known in the art of information science. In a preferred embodiment, the error code type parameter selects between Reed-Solomon codes encoding N payload bits using a block of M transmitted bits, where M is greater than or equal to N. However, in alternative embodiments, other error codes could be used, such as Viterbi (concatenated) Turbo codes, MD5 or secure hash codes, or other error codes adaptable to variations in channel, subscriber, or time.

1 The error code parameter allows the BSC 120 to optimize a communication link
2 with a selected CPE 130 in response to both interference effects and multipath ef-
3 fects.

4
5 Figure 8 shows a chart of reduced frame loss ratio provided by the BSC 120
6 using modulation and error code selection.

7
8 A chart 800 includes an X-axis 810 representing a carrier to noise ratio
9 (CNR) in decibels (db), a Y-axis 820 representing a frame-loss ratio (FLR), and a set of
10 plotted curves 830 each representing a function coupling CNR on the X-axis 810 with
11 FLR on the Y-axis 820 for a selected value of modulation parameter and error code pa-
12 rameter. The modulation parameter is shown as 16QAM; the error code parameter can
13 vary among various strengths of Reid-Solomon codes.

14
15 In a preferred embodiment, the BSC 120 selects, for each communication
16 link with selected CPE 130, a modulation selection parameter for the communication
17 link. It would be clear to those of ordinary skill in the art, after perusal of this applica-
18 tion, that selection of the modulation parameter and the error code parameter, is a tool for
19 the BSC 120 to maximize the value of its communication link with each selected CPE
20 130.

- **equalization** — When BSC 120 and the CPE 130 exchange information, the communication link between the two imposes an impulse response, so that a signal which is transmitted from the sender to the receiver is transformed in a substantially nonlinear manner. The impulse response is primarily due to multipath effects of communication between the sender and receiver, but can also be due to other frequency-diverse effects such as weather.

In a preferred embodiment, the BSC 120 and the CPE 130 include an equalizer element, which attempts to invert the impulse response of the communication link by pre-conditioning the signal before transmission. The equalizer element includes a sequence of coefficients for use in a finite impulse response (FIR) filter, or may include a sequence of coefficients for use in a polynomial for determining values for an infinite impulse response (IIR) filter. The equalization parameter thus includes the sequence of coefficients for the filter used for pre-conditioning the signal before transmission.

The equalization parameter allows the BSC 120 to optimize a communication link with a selected CPE 130 in response to multipath effects.

In a preferred embodiment, physical parameters and MAC parameters include at least the following MAC parameters:

- 1 • **message size** — As described in the Incorporated Disclosures, the BSC 120 and
2 the CPE 130 exchange information using (downstream or upstream) payload ele-
3 ments, each of which includes header information and payload information. The
4 message size parameter includes a value for the amount of payload information to
5 be included in each payload element; this value can vary from a relatively small
6 number of payload bytes to the maximum number of payload bytes allowed by the
7 network (layer 2) protocol, typically about 1500.

8
9 In a preferred embodiment, the message size parameter is primarily respon-
10 sive to the bit error rate (BER) experienced for the communication link between the BSC
11 120 and the CPE 130. When the bit error rate is relatively small, the message size pa-
12 rameter can be set to be relatively large, so as to reduce the amount of overhead for
13 header information in each payload element. However, when the bit error rate is rela-
14 tively larger, the message size parameter can be set to be relatively smaller, so as to re-
15 duce the amount of overhead for lost payload elements due to errors in one or more sym-
16 bols of transmitted payload elements. The modulation selection parameter allows the
17 BSC 120 to optimize a communication link with a selected CPE 130 in response to inter-
18 ference effects.

19
20 Those skilled in the art will recognize, after perusal of this application, that
21 there is a relationship between the modulation type, error code type, and message size.
22 Thus, where the modulation type allocates relatively fewer bits per symbol, the likelihood

1 of error for any particular symbol is relatively lower, and the bit error rate will also be
2 relatively lower. Similarly, where the error code type allocates relatively more error de-
3 tection or correction bits per symbol, the likelihood of error for a particular symbol is also
4 relatively lower, and the bit error rate will also be relatively lower. In those cases where
5 the bit error rate is relatively lower, the message size parameter can be set to a relatively
6 larger value.

7
8 Figure 9 shows a chart of increased throughput ("goodput") provided by the
9 BSC 120 using message size selection.

10
11 A chart 900 includes an X-axis 910 representing a message size or frame
12 length for data transmission between the BSC 120 and the selected CPE 130, a Y-axis
13 920 representing a throughput value (in kilobits per second), a set of plotted curves 930
14 each representing a function coupling message size on the X-axis 910 with throughput on
15 the Y-axis 920 for a known value of bit error rate (BER).

16
17 In a preferred embodiment, the BSC 120 selects, for each communication
18 link with selected CPE 130, a message size parameter for the communication link. It
19 would be clear to those of ordinary skill in the art, after perusal of this application, that
20 selection of the message size parameter, is a tool for the BSC 120 to maximize the value
21 of its communication link with each selected CPE 130.

- 1 • **acknowledgment** and **retransmission** — As described in the Incorporated Dis-
2 closures, the BSC 120 and the CPE 130 exchange information using acknowledg-
3 ment (ARQ) messages, so as to indicate to the sender whether or not the receiver
4 has accurately received any particular payload element. If a particular payload
5 element is not received, the sender can decide to retransmit that payload element a
6 number of times, so as to attempt to having received correctly. The acknowledg-
7 ment parameter selects how frequently acknowledgment messages are used to re-
8 ply to payload elements, and thus how frequently to let the sender know whether
9 those payload elements have been received. Similarly, the retransmission pa-
10 rameter selects how persistently the sender will attempt to send or resend payload
11 elements to the receiver.

12 The acknowledgement parameter allows the BSC 120 to optimize a com-
13 munication link with a selected CPE 130 in response to both interference effects and
14 multipath effects.

15
16
17 Those skilled in the art will recognize, after perusal of this application, that
18 there is a relationship between the application in use by the layer 5 application protocol
19 and the choice of acknowledgment and retransmission parameters. For example, where
20 the application includes voice transmission or other streaming media, there is little value
21 in retransmitting any particular payload element, as the time for decoding and presenting
22 that payload element is usually well passed by the time that particular payload element

1 can be retransmitted by the sender and received by the receiver. On the contrary, for ex-
2 ample, where the allocation includes file data transfer, there is relatively greater value in
3 retransmitting each lost payload element, as each and every payload element is generally
4 required for useful reception of the entire file data transfer.

5
6 Those skilled in the art will also recognize, after perusal of this application,
7 that there is a relationship between choice of class of service (CoS) and quality of service
8 (QoS) for other protocol layers and the choice of acknowledgment and retransmission pa-
9 rameters. For example, where the application includes data transfer or backup related
10 applications, it might be desirable to assure that data sent from one device to another is
11 well-assured to be correct. Thus, in such case, it might be desirable to adjust acknowl-
12 edgment and retransmission parameters so that data transfer is assured to be as correct as
13 possible as soon as possible.

14
15 Figure 10 shows a chart of increased throughput provided by the BSC 120
16 using acknowledgement and retransmission parameter selection.

17
18 A chart 1000 includes an X-axis 1010 representing a packet error rate
19 (PER) for data transmission between the BSC 120 and the selected CPE 130, a Y-axis
20 1020 representing a normalized throughput value, and a set of plotted curves 1030 each
21 representing a function coupling PER on the X-axis 1010 with throughput on the Y-axis

1 1020 in response to whether dynamic acknowledgement and retransmission parameter
2 selection is used or not.

3
4 In a preferred embodiment, the BSC 120 selects, for each communication
5 link with selected CPE 130, a message size parameter for the communication link. It
6 would be clear to those of ordinary skill in the art, after perusal of this application, that
7 selection of whether or not to use dynamic acknowledgement and retransmission is a tool
8 for the BSC 120 to maximize the value of its communication link with each selected CPE
9 130.

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- **TDD duty cycle** — As described in the Incorporated Disclosures, the BSC 120 and the CPE 130 exchange information using a downstream portion and an upstream portion of a TDMA transmission frame. The TDD duty cycle parameter selects how much of the TDMA transmission frame is allocated for downstream information transfer and how much of the team a transmission frame is allocated for upstream information transfer.

18 The TDD duty cycle parameter allows the BSC 120 to optimize a communication
19 link with a selected CPE 130 in response to interference effects.

20
21 As described below, the BSC 120 maintains these physical parameters and
22 MAC parameters, and adaptively modifies them with changing conditions on the com-

1 munication link between the BSC 120 and the CPE 130. Thus, when the BSC 120 no-
 2 tices a change in characteristics of the communication link, it does not immediately alter
 3 the physical parameters and MAC parameters to correspond exactly to the new charac-
 4 teristics of the communication link. Rather, the BSC 120 maintains a sequence (of at
 5 least one) past sets of values of these parameters, and modifies the most recent set of pa-
 6 rameters using the new characteristics, so as to adjust the set of parameters dynamically
 7 while allowing sets of values of these parameters to have persistent effect on future val-
 8 ues.

9
 10 In a preferred embodiment, the BSC 120 records each current value for the
 11 physical parameters and MAC parameters, determines exact values for the physical pa-
 12 rameters and MAC parameters in response to characteristics of the communication link,
 13 and adaptively selects new values for the physical parameters and MAC parameters (thus,
 14 for the next TDMA frame) by linearly mixing current values with dynamic values. Op-
 15 eration of this technique is shown in the following equation 150:

$$\text{value}_{\text{new}} \leftarrow 1 - \alpha * \text{value}_{\text{current}} + \alpha * \text{value}_{\text{exact}} \quad (150)$$

19
 20 where

- 21
- 22 • $\text{value}_{\text{new}}$ = the new value of each parameter, for the next TDMA frame;

- 1
- 2 • value_{current} = the current value of each parameter, for the most recent TDMA
- 3 frame;
- 4
- 5 • value_{exact} = the dynamic exact value of each parameter, determined in response to
- 6 characteristics of the communication link;
- 7
- 8 and
- 9 • alpha = a hysteresis parameter for determining how fast to respond to changes in
- 10 characteristics of the communication link.

11 In a preferred embodiment, the value of alpha is specific to each individual

12 physical parameter and MAC parameter.

13 *Method of Operation*

14

15

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17 Figure 11 shows a time division duplex frame used in a system as in figure

18 1.

19

20 A time division duplex (TDD) frame 1100 includes a time-synchronization

21 portion 1110, a first guard time 1120, a downstream portion 1130, a second guard time

22 1140, a status-synchronization portion 1150, and an upstream portion 1160.

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The time-synchronization portion 1110 includes a first symbol 1111 indicating the beginning of the TDD frame 1100, and a sequence of parameter setting values 1112 for each CPE 130. The BSC 120 uses the parameter setting values 1112 to inform each selected CPE 130 individually and separately of (a) the PHY and MAC parameters the BSC 120 is using to send messages to that selected CPE 130, and (b) the PHY and MAC parameters the selected CPE 130 should use to send messages to the BSC 120 during its allocated part of the upstream portion 1160.

The first guard time 1120 includes a time duration sufficient for the BSC 120 to assure that all CPE 130 do not interfere with each other when receiving from the BSC 120 or sending to the BSC 120.

The downstream portion 1130 includes a sequence of downstream payload elements 1131, each sent by the BSC 120 to a selected CPE 130. The BSC 120 determines a length for each of these downstream payload elements 1131 and sends that information with the parameter setting values 1112 in the time-synchronization portion 1110. In alternative embodiments, the BSC 120 may divide the CPE 130 into classes and allocate one or more downstream payload elements 1131 for each class of CPE 130. For example, the BSC 120 may allocate one or more downstream payload elements 1131 for broadcast or multicast messages.

1 The second guard time 1140 includes a time duration sufficient for the BSC
2 120 to assure that the downstream portion 1130 and the status-synchronization portion
3 1150 do not interfere.

4
5 The status-synchronization portion 1150 includes a sequence of status in-
6 formation so that the BSC 120 can agree with each selected CPE 130 regarding higher-
7 level protocol status out-of-band from those higher-level protocols.

8
9 Similar to the downstream portion, the upstream portion 1160 includes a
10 sequence of upstream payload elements 1161, each sent by a selected CPE 130 to the
11 BSC 120. The BSC 120 (not the CPE 130) determines a length for each of these up-
12 stream payload elements 1161 and sends that information with the parameter setting val-
13 ues 1112 in the time-synchronization portion 1110. In alternative embodiments, the BSC
14 120 may divide the CPE 130 into classes and allocate one or more upstream payload
15 elements 1131 for each class of CPE 130, such as for upstream bandwidth contention.

16
17 Figure 12 shows a process flow diagram of a method for operating a system
18 using adaptive point to multipoint wireless communication in a wireless communication
19 system.

20
21 A method 1200 includes a set of flow points and a set of steps. The system
22 100 performs the method 1200. Although the method 1200 is described serially, the steps

1 of the method 1200 can be performed by separate elements in conjunction or in parallel,
2 whether asynchronously, in a pipelined manner, or otherwise. There is no particular re-
3 quirement that the method 1200 be performed in the same order in which this description
4 lists the steps, except where so indicated.

5
6 At a flow point 1210, the BSC 120 and the CPE 130 are ready to begin a
7 TDMA frame.

8
9 At a step 1211, the BSC 120 and the CPE 130 conduct communication us-
10 ing a TDMA frame. As part of this step, the BSC 120 directs the CPE 130 regarding
11 which physical parameters and MAC parameters to use.

12
13 At a step 1212, the BSC 120 determines characteristics of the communica-
14 tion link with the CPE 130, in response to performance of the communication during the
15 previous TDMA frame.

16
17 At a step 1213, the BSC 120 determines exact values for the physical pa-
18 rameters and MAC parameters in response to characteristics of the communication link.

19
20 At a step 1214, the BSC 120 determines new values for the physical pa-
21 rameters and MAC parameters in response to results of the previous step, and perform-
22 ance of the equation 150.

1
2 After this step, the BSC 120 and the CPE 130 have performed one step of
3 sending and receiving information using a TDMA frame. The flow point 1210 is reached
4 repeatedly and the steps thereafter are performed repeatedly, for each TDMA frame.
5

6 *Generality of the Invention*
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8 The invention has general applicability to various fields of use, not neces-
sarily related to the services described above. For example, these fields of use can in-
clude one or more of, or some combination of, the following:

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- The invention is applicable to other forms of wireless communication, such as fre-
quency division multiple access (FDMA) or code division multiple access
(CDMA, also known as spread spectrum communication);
 - The invention is applicable to any non-wireless communication, in which relative
effectiveness or efficiency of communication can be achieved from dynamically
adjusting communication parameters, such as physical parameters or MAC pa-
rameters. For example, the invention can be generalized to non-wireless commu-
nication using modems in which equalization parameters are to be dynamically
adjusted.
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- 1 • The invention is applicable to other wireless communication systems, such as sat-
2 ellite communication systems and (microwave tower or other) point to point
3 transmission systems.
4
- 5 • The invention is applicable to both fixed wireless communication systems, in
6 which customer premises equipment do not move relative to the BSC 120, and to
7 mobile wireless communication systems, and which customer premises equipment
8 move substantially relative to the BSC 120.

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